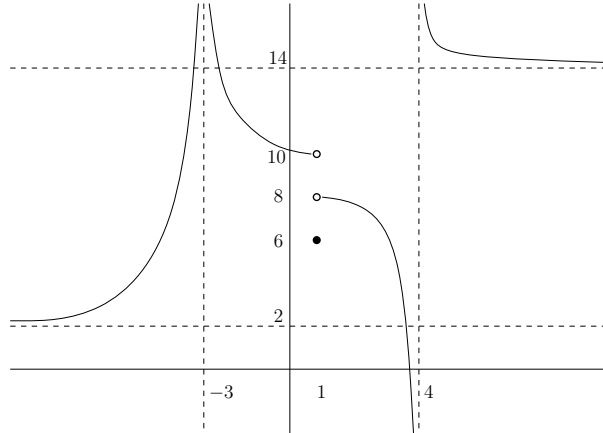


# Calculus I Exam One

Name: \_\_\_\_\_

Please show all work on these problems. Use of a calculator is not permitted.

1. Based on the graph of  $f$  given below, find the following.



(a)  $\lim_{x \rightarrow -3^-} f(x)$

(h)  $f(1)$

(b)  $\lim_{x \rightarrow -3^+} f(x)$

(i)  $\lim_{x \rightarrow 4^-} f(x)$

(c)  $\lim_{x \rightarrow -3} f(x)$

(j)  $\lim_{x \rightarrow 4^+} f(x)$

(d)  $f(-3)$

(k)  $\lim_{x \rightarrow 4} f(x)$

(e)  $\lim_{x \rightarrow 1^-} f(x)$

(l)  $f(4)$

(f)  $\lim_{x \rightarrow 1^+} f(x)$

(m)  $\lim_{x \rightarrow \infty} f(x)$

(g)  $\lim_{x \rightarrow 1} f(x)$

(n)  $\lim_{x \rightarrow -\infty} f(x)$

Find the following limits.

2.  $\lim_{x \rightarrow 4} \frac{x^2 + 2x - 24}{x^2 - 16}$ .

3.  $\lim_{x \rightarrow -\infty} \frac{-3x^7 - 2x^4 + 8}{-5x^4 - 9}$

4.  $\lim_{x \rightarrow \infty} \frac{\sqrt{64x^{10} - 6x^7 + 2}}{7x^5 - 9x^3 + 5}$

5.  $\lim_{x \rightarrow 25} \frac{\sqrt{x}-5}{x+1}$

6.  $\lim_{x \rightarrow -\infty} x^7 + x^6$

7.  $\lim_{x \rightarrow 3} \frac{\frac{1}{x}-\frac{1}{3}}{x-3}$

8.  $\lim_{x \rightarrow 4^+} \frac{7-x}{x-4}$

9.  $\lim_{x \rightarrow 4} \frac{x-4}{\sqrt{x}-2}$

10. Find all vertical and horizontal asymptotes of the function  $f(x) = \frac{3x^2+12x}{x^2-x-20}$ .

11. Calculate  $\frac{6e^{4x} - 6}{12x}$  for  $x = 0.1, 0.01, 0.001, 0.0001$ . Use this information to estimate  $\lim_{x \rightarrow 0^+} \frac{6e^{4x} - 6}{12x}$ .

12. Suppose  $f(x) = 5e^{-2x}$ .

(a) Find  $\lim_{x \rightarrow \infty} f(x)$  and  $\lim_{x \rightarrow -\infty} f(x)$ .

(b) Find all of this function's vertical and horizontal asymptotes.